

**LITTLE FLOWER CONVENT HIGH SCHOOL**

STD	SUBJECT	EXAM	DATE	MARKS
X	MATHS-PAPER 2	PRELIMINARY-2021 -22	21-01-2022	40

- NOTE :**
- (i) All questions are compulsory.
  - (ii) The numbers to the right of the questions indicate full marks.
  - (iii) In case of MCQ's [Q. No. 1A ], only the first attempt will be evaluated and will be given credit.
  - (iv) For every MCQ, the correct alternative (A), (B), (C) or (D) in front of sub-question number is to be written as an answer.
  - (v) Draw proper figures for answers wherever necessary.
  - (vi) The marks of construction should be clear and distinct. Do not erase them.
  - (vii) Diagram is essential for writing the proof of the theorem.

**Q. 1. ( A )** Four alternative answers are given for each of the following sub-questions. Choose the correct alternative and write the letter of the alphabet of that answer: [4]

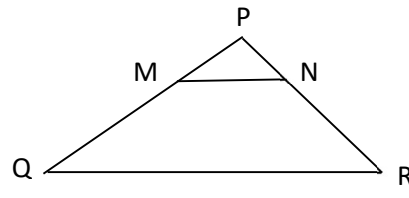
(i) In given figure, seg MN || seg QR, then which of the following statements is true?

[A]  $\frac{PM}{MQ} = \frac{PN}{PR}$

[B]  $\frac{MQ}{PM} = \frac{NR}{PN}$

[C]  $\frac{PM}{PQ} = \frac{PN}{NR}$

[D]  $\frac{PM}{PN} = \frac{PQ}{NR}$



(ii) Out of the following which is the Pythagorean triplet?

- [A] ( 2,3,4)    [B] (3,4,5)    [C] (1,5,10)    [D] (5,6,4)

(iii)  $\angle ABC$  is inscribed in arc ABC of a circle with centre O. If  $\angle ABC = 75^\circ$ , find  $m(\text{arc } ABC)$ .

- [A]  $75^\circ$                       [B]  $150^\circ$                       [C]  $210^\circ$                       [D]  $215^\circ$

(iv) Distance of point (-4,3), from the origin is .....

- [A] 6                      [B] 5                      [C] 1                      [D] -5

**Q. 1. ( B )** Solve the following sub-questions : [4]

(i) Base of a triangle is 12 and height is 7. Base of another triangle is 14 and height is 8.

Find the ratio of areas of these triangles.

(ii) Find the diagonal of a rectangle whose length is 20cm and breadth is 15cm.

(iii)  $\square MRPN$  is cyclic,  $\angle R = 135^\circ$ . Find  $m\angle N$ .

(iv) If  $\sin\theta = \frac{12}{13}$ , find the value of  $\cos\theta$ .

**Q. 2. (A) Complete and write any two of the following activities:**

[4]

(i) In figure,  $\angle ABC = 90^\circ$ , seg  $BD \perp$  seg  $AC$ ,  $AD = 9$ ,  $DC = 25$ . Find  $BD$ .

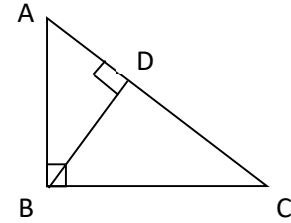
→ In  $\triangle ABC$ , seg  $BD \perp$  seg  $AC$ .

$$BD^2 = \square \times DC \text{ ----- geometric mean property}$$

$$BD = \sqrt{\square \times DC}$$

$$= \sqrt{9 \times \square}$$

$$BD = \square$$



(ii) In figure, chords  $AB$  and  $CD$  intersect at  $M$ .  $m \angle ADC = 32^\circ$ ,  $m \angle BMD = 68^\circ$ . Find  $m$  (arc  $BD$ )

→  $\angle DMB$  is exterior angle of  $\triangle AMD$ ,

By remote interior angles' theorem,

$$m \angle DAB = m \angle DAM = 68^\circ - \square^\circ$$

$$\therefore \angle DAB = \square^\circ$$

$\angle DAB$  is inscribed angle and intersects arc  $BD$

$$m \angle DAB = \frac{1}{2} m(\text{arc } BD) \text{ ----- } \square \text{ Reason}$$

$$\therefore m(\text{arc } BD) = 2m \angle DAB$$

$$\therefore m(\text{arc } BD) = \square^\circ$$

(iii) If  $\operatorname{cosec} \theta = \frac{25}{7}$ , complete the following activity to find the value of  $\cot \theta$

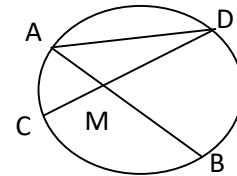
$$\rightarrow 1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$$

$$1 + \cot^2 \theta = \left[ \frac{\square}{\square} \right]^2$$

$$\therefore \cot^2 \theta = \frac{625}{49} - \square$$

$$\therefore \cot^2 \theta = \frac{625-49}{49} = \frac{\square}{49}$$

$$\therefore \cot \theta = \frac{\square}{7} \text{ ----- (by taking square roots)}$$



**Q. 2. (B) Solve any four of the following sub-questions:**

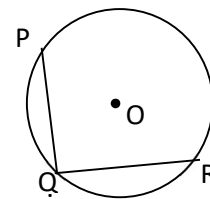
**[8]**

- (i) If  $\triangle DEF \sim \triangle MNP$ ,  $A(\triangle DEF) = 100$ ,  $A(\triangle MNP) = 225$ , then find  $\frac{DE}{MN}$
- (ii) In  $\triangle XYZ$ ,  $\angle Y = 90^\circ$ ,  $\angle X = 30^\circ$ ,  $XZ = 18$ , then find  $XY$  and  $YZ$ .
- (iii) The radii of two circles are 3cm and 2.5cm. Draw figure of these circles touching each other externally. Also, find the distance between their centres.
- (iv) If point P divides the line segment AB with A (-4,8) and B (-2,6) in the ratio 3: 1, find the y co ordinate of point P.
- (v) If  $\sin\theta = \frac{\sqrt{3}}{2}$ , find  $\theta$ ,  $\operatorname{cosec}\theta$ ,  $\cos\theta$ ,  $\tan\theta$ .

**Q. 3. (A) Complete and write any one of the following activities:**

**[3]**

(i) Observe the figure and answer the following:



P, Q, R are any points on the circle with centre O.

$$m(\text{arc PQ}) = m(\text{arc QR}) = 75^\circ$$

Find  $m(\text{arc PQR})$ ,  $m(\text{arc PR})$  and show chord  $PQ \cong$  chord  $QR$ .

$$\rightarrow m(\text{arc PQ}) = m(\text{arc QR}) = 75^\circ \text{-----given}$$

$$m(\text{arc PQR}) = m(\text{arc } \boxed{\phantom{00}}) + m(\text{arc } \boxed{\phantom{00}}) \text{-----property of sum of measures of arcs.}$$

$$\therefore m(\text{arc PQR}) = \boxed{\phantom{00}}^\circ$$

$$m(\text{arc PR}) = 360^\circ - m(\text{arc } \boxed{\phantom{00}}) = \boxed{\phantom{00}}^\circ$$

$$m(\text{arc PQ}) = m(\text{arc QR}) \text{-----given}$$

$$\therefore \text{chord PQ} \cong \text{chord QR} \text{-----} \boxed{\phantom{000000}} \text{ reason}$$

**(ii) Show that points P (1,2), Q (-2,3) and R (4,1) are collinear.**

$\rightarrow$  If the sum of any two distances out of  $d(P, Q)$ ,  $d(Q, R)$  and  $d(P, R)$  is equal to the third, then the three points P, Q and R are collinear.

$\therefore$  we will find  $d(P, Q)$ ,  $d(Q, R)$  and  $d(P, R)$ .

$$d(P, Q) = \boxed{\phantom{0000}} \text{----- (I)-----find distance by using distance formula}$$

$$d(Q, R) = \boxed{\phantom{0000}} \text{-----(II)}$$

$$d(P, R) = \boxed{\phantom{0000}} \text{-----(III)}$$

From I, II, and III,

$$\boxed{\phantom{0000}} + \boxed{\phantom{0000}} = 2\sqrt{10}$$

$$\therefore d(P, Q) + d(P, R) = d(\boxed{\phantom{0000}})$$

$\therefore$  Points P, Q, R are collinear.

**Q. 3. (B) Solve any two of the following sub-questions:**

[ 6 ]

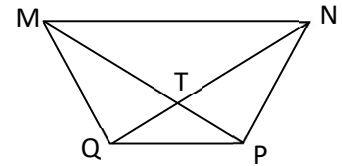
- (i) Prove that, tangent segments drawn from an external point to the circle are congruent.
- (ii) Draw a circle of radius 4.2cm and centre O. Mark a point B at a distance of 7.5cm from the centre. Draw tangents to the circle from point B.

- (iii) In  $\square$  MNPQ, seg MN  $\parallel$  seg QP.

Diagonal MP and diagonal QN intersect each other in point T.

Then show that:

$$\frac{MT}{MN} = \frac{PT}{PQ}$$



- (iv) In  $\triangle$ ABC, G (6, -2) is the centroid. If A (3, -5) and B (4, 3), then find the co ordinates of point C.

**Q. 4. Solve any two of the following sub-questions:**

[8]

- (i) The line segment AB is divided into five congruent parts at P, Q, R and S, such that A – P – Q – R – S – B. If point Q (12,14) and S (4,18) are given, find the co ordinates of A, P, R and B.

- (ii)  $\triangle$ SPQ  $\sim$   $\triangle$ STR. In  $\triangle$ SPQ, SP = 5.8cm,  $\angle$ QSP =  $60^\circ$ , SQ = 4.6cm.

$$\frac{SP}{ST} = \frac{5}{3} . \text{ Construct } \triangle$$
STR

- (iii) Prove that, if two lines containing chords of a circle intersect each other outside the circle, then the measure of angle between them is half the difference in measures of the arcs intercepted by the angle.

**Q. 5. Solve any one of the following sub-questions:**

[3]

- (i) The lengths of perpendicular sides of right triangle are 8cm and 6cm.

Draw a circle passing through all three vertices of a triangle, also draw a tangent to the circle at any one vertex of the triangle.

- (ii) Anju and Manju started walking to the West and to the North respectively, from the same point and at the same speed. After 2 hours distance between them was  $17\sqrt{2}$  km. Find their speed per hour.

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